

Burzio (2002a,b) **Representational Entailments Hypothesis** (REH):

⇒	A	B	C
A	1	1	1
B	1	1	1
C	1	1	1

Mental representations of linguistic expressions are sets of entailments.

Entailment matrix for a representation ABC: 1= entailment

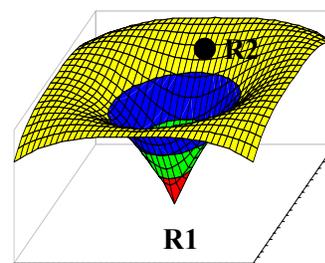
Each of A, B, C can be phonemes in a sequence, features within a phoneme, or other.

Yields attraction over distance

Entailments violated by ¬C in some R2, given an R1= A B C:

A ⇒ C	
B ⇒ C	A ⇒ C
A	A
B	¬B
¬C	¬C

Varying the structure of R2:



Take-over of OT FAITH constraints ~~IO-FAITH~~ Attraction: Non-Derived Environment Blocking

~~OO-FAITH~~ Attraction: Lexical Conservatism

Attraction also handles:

Syncretism in Morphology

* enhances the similarity relation, yielding neutralization

gli	gli + lo*	⇒ glielo
le	le + lo*	

Perceptual effects (categorical perception/ perceptual magnet): percept attracted to category

Dispersion Theory: Maximal distance = maximal harmony (minimal attraction)

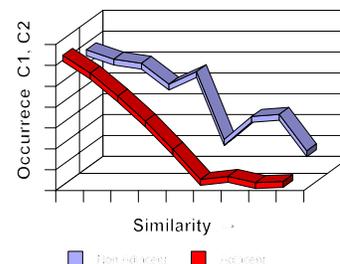
The REH also yields a theory of **surface-to-surface morphology**. Entailment summation across the lexicon yields subcategorization frames like **-al** ⇒ /N __

Extending attraction by extending the scope of ‘similarity’:

In a sequence ABC, A and B are sequentially similar, as are B and C.

Empirical evidence:

Frisch et al. (2004): trade-offs between feature-similarity and sequential proximity in **OCP effects in Arabic** (chart based on their Table IV, p. 203).



C_αV_α: Assimilations of Cs to adjacent Vs are common

(palatalizations, spirantizations, voicing), and seem to require some independent similarity C_βV_β. E.g. Spanish spirantization: Cu[β]a/ co[p]a (same voicing ⇒ same continuancy).

*C_α X V_α: Comparable long distance assimilations are unattested.

C_α X C_α: Long distance assimilations between Cs are attested, but only under strong similarity: Rose and Walker (2004). Cf. also Vowel harmony, often ‘parasitic’.

↑↑		Generalized Similarity			restrictions ↗
		Max: within Cs or Vs	Dispersion Theory (inventories)	LongDist. effects: Rose and Walker	
featural proximity	Min: across C, V	no restriction	full inventory	Local Assim./Dissim.	
	freedom ↖	Zero: in the same language	Min: in the same sequence	Max: adjacent/ articulatorily local	
sequential proximity →→					

REH: very powerful in ability to subsume much traditional theoretical machinery, **but** no prediction of which components may cluster, yielding smaller units:

ABC/ AB \neg C = clustering of A, B violates 2 entailments

ABC/ A \neg BC = clustering of A, C violates 2 entailments also

However, while morphemes are clusters of phonemes, by and large there are no discontinuous morphemes, like a hypothetical *in-.....-y*, such that *in-accurac-y* would just mean ‘inaccurate’.

REH seems to fail in helping understand the character of ‘inventories’, or does it?

Scale of units	Inventory?	GS?
distinctive features	Yes, determined by articulation/ perception	
segments (phonemes)	Yes, not all features combine freely: [+back] \Rightarrow [+ round]	(y)
bi-phones	Approx.: only homogeneous: diphthongs or C clusters	y
n>2-phones	No	n
morphemes	Adjacent phonemes: in-, -al, -ment, ...	y
(phonemes + meaning)	Non-adjacent but homogeneous for major class (Semitic): k t b u i	y

Burzio (2005, 77-81) offers a crude set of inferential steps to derive as a corollary of REH/ attraction:

the **Binding corollary:** Any two components A, B (of a representation ‘X, A, B, Y’ that includes them) ‘bind’ together to the extent that they are similar. That is, the strength of the entailments $A \Rightarrow B$, $B \Rightarrow A$ under the REH is determined by the generalized-similarity of A and B.

Note: Similarity also establishes attraction, so that A, B could also undergo either assimilation or dissimilation (whatever further similarity or dissimilarity results will determine the binding effect).

The **binding corollary** thus unravels the ontology of units: there are phonemes, and there are only morphemes of very specific types; there are no diphones, except (approx.) diphthongs and C clusters.

Proof?

A. Wayment (in progress) provides proof in terms of a neural net simulation.

E.g. Analysis of R (round) and B (back) into putative acoustic sub-features as a test case for the more general situation of partial similarity.

	identical			different				
	a1	a2	a3	a4	a5	a6	a7	a8
+R	1	1	1	-1	1	-1	-1	-1
~R	-1	-1	-1	-1	-1	1	-1	-1
+B	1	1	1	1	-1	-1	1	-1
~B	-1	-1	-1	-1	-1	-1	-1	1

The REH = Hopfield net: each unit is connected to each of the others. Above entailment matrix = weight matrix

Representation A, B, C = a ‘vector’ V

Matrix: Outer product (Tensor product) of V with itself: $V \otimes V$

	A	B	C
A	1	1	1
B	1	1	1
C	1	1	1

Applying this now to [round] and [back], putting vowel height aside and assuming that we are dealing only with high vowels, we have:

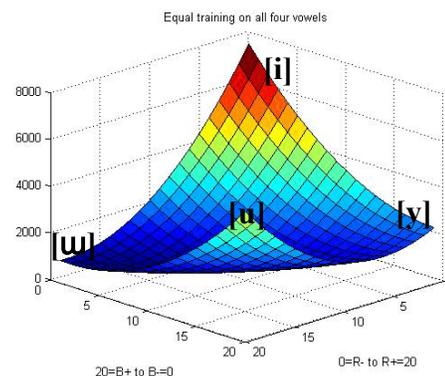
	~B	+B
+R	y	u
~R	i	ɯ

Thus, we have two vectors: αR and βB (α , β each varying over +, ~), which co-occur in any one vowel. The Hopfield net implementation of the REH, gives, for each vowel, 4 weight matrices:

$\alpha R \otimes \alpha R$	Outer product of αR with itself (each internal component of αR entails the others)
$\beta B \otimes \beta B$	Outer product of βB with itself (each internal component of βB entails the others)
$\alpha R \otimes \beta B$	Outer product of αR with βB (the vector αR entails the vector βB)
$\beta B \otimes \alpha R$	Outer product of βB with αR (the vector βB entails the vector αR). Same as above.

The REH-based representation of each of the four vowels: the total set of entailments (weight matrix) for an αR co-occurring with a βB , equals the sum of the four weight matrices.

The predicted clustering of backing and rounding would now consist of some **greater harmony** of the sum matrices for $+R$, $+B$ ($=[u]$) and $\sim R$, $\sim B$ ($=[i]$) compared with the matrices for the other two vowels.



Indeed:

The proof generalizes to other cases (the specific acoustic features a1-a8 are arbitrary and only serve to implement some degree of similarity/ dissimilarity).

Hence: **The ontology of units (phonemes/ morphemes) is inferrable from the binding of subunits under generalized similarity.**

Conclusion: The resources of continuous mathematics, that include the ability to perform summations are no more dispensable in the study of morpho-phonology than they are in the study of perception. Summation is inherent in the notion of distance in multidimensional space, which in turn is critical to understanding a broad range of effects that include: Non-Derived Environment Blocking, Lexical Conservatism, morphological syncretism, and the nature of both segmental inventories and inventories of morphemes.

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